## What is claimed is:

1. A method for measuring a true mean differential group delay  $\langle \tau \rangle$  of at least one length of optical fiber comprising the steps of:

measuring a mean square differential group delay  $\langle \tau^2 \rangle_B$  averaged over a finite bandwidth B of the source using a polarization mode dispersion measurement apparatus;

calculating a root mean square differential group delay in accordance with  $\sqrt{\left\langle \tau^2 \right\rangle_{\!\scriptscriptstyle B}}$  ; and

applying a systematic correction factor  $\epsilon$  to  $\sqrt{\langle \tau^2 \rangle_B}$  to calculate  $\langle \tau \rangle$ , the application of  $\epsilon$  minimizing a systematic error caused by the finite bandwidth B of the source, where  $\tau$  is in units of second, B in units of radian/second.

2. The method of Claim 1, further including the step of applying the systematic correction factor ε in accordance with:

$$\langle \tau \rangle = \sqrt{\frac{8}{3\pi} \langle \tau^2 \rangle_B} + \epsilon,$$
 (16a)

where  $\pi$  is substantially equal to 3.14159 and  $\langle \tau \rangle$  is in units of second,  $\langle \tau^2 \rangle_B$  is in units of second<sup>2</sup>.

3. The method of Claim 2, wherein the finite bandwidth B is much greater than the inverse of the root mean square differential group delay  $\sqrt{\langle \tau^2 \rangle_B}$ :

$$B >> \frac{1}{\sqrt{\langle \tau^2 \rangle_R}}$$
,

further wherein  $\varepsilon$  is defined by the following equation:

$$\varepsilon = \frac{8}{9\sqrt{2}} \frac{1}{B}, \quad \text{and}$$
 (16b)

where B is in units of radian/second, and  $\tau$  and  $\sqrt{\langle \tau^2 \rangle_B}$  are in units of second.

- 4. The method of Claim 1, wherein the polarization mode dispersion measurement apparatus used to measure the mean square differential group delay  $\langle \tau^2 \rangle_B$  comprises a time-domain measurement apparatus.
- 5. The method of Claim 4, wherein the time-domain measurement apparatus is an interferometric device.
- 6. The method of Claim 1, wherein the polarization mode dispersion measurement apparatus used to measure the mean square differential group delay  $\langle \tau^2 \rangle_B$  comprises a frequency-domain measurement apparatus.
- 7. The method of Claim 6, wherein the frequency-domain measurement apparatus is a polarimeter.
- 8. The method of Claim 7, further comprising the step of applying one of a Jones Matrix Eigenanalysis, Poincaré Sphere Analysis, and Müller Matrix Method to calculate the mean square differential group delay  $\langle \tau^2 \rangle_R$ .
- 9. The method of Claim 1, wherein the at least one length of optical fiber is an optical fiber link in an optical telecommunication network.
- 10. The method of Claim 1, wherein the at least one length of fiber is an optical fiber route in an optical telecommunication network.
- 11. A method for measuring a mean differential group delay  $\langle \tau \rangle$  of at least one length of optical fiber, comprising the steps of:

characterizing a polarization mode dispersion vector as a function of frequency using a frequency-domain polarization mode dispersion measurement apparatus;

calculating a second-order polarization mode dispersion vector  $\vec{\tau}_{\omega}$  as a function of frequency by calculating a derivative with respect to frequency of the polarization mode dispersion vector;

calculating a mean of a square root of a magnitude of the second-order polarization mode dispersion vector  $\vec{\tau}_{\omega}$  to obtain a first result, according to  $\langle |\vec{\tau}_{\omega}|^{1/2} \rangle$ , wherein  $|\vec{\tau}_{\omega}|$  represents the magnitude of the second-order polarization mode dispersion vector; and multiplying a proportionality coefficient  $A_2$  of the second-order polarization mode dispersion vector  $\vec{\tau}_{\omega}$  by the first result to calculate the mean differential group delay  $\langle \tau \rangle$  in accordance with the following equation:

$$A_2 \left\langle \left| \vec{\tau}_{\omega} \right|^{1/2} \right\rangle = \left\langle \tau \right\rangle, \tag{21}$$

where  $\tau$  and  $\langle \tau \rangle$  are in units of second<sup>2</sup>,  $|\tau_{\omega}|$  is in units of second,  $\omega$  is in units of radian/second, and  $A_2$  is dimensionless.

- 12. The method of Claim 11, wherein  $A_2$  is substantially equal to 1.37.
- 13. The method of Claim 11, wherein the frequency-domain polarization mode dispersion measurement apparatus is one of a polarimetric device and a Fixed Analyzer device.
- 14. The method of Claim 11, wherein the at least one length of fiber is a single fiber link.
- 15. The method of Claim 11, wherein the at least one length of fiber is a fiber route.
- 16. A method for measuring a mean differential group delay  $\langle \tau \rangle$  of at least one length of fiber, comprising the steps of:

measuring a magnitude of a polarization mode dispersion vector  $|\tau_{\omega}|$  as a function of frequency, using a frequency-domain polarization mode dispersion measurement apparatus, the magnitude of the polarization mode dispersion vector  $|\tau_{\omega}|$  being a scalar differential group delay;

calculating a frequency derivative of the scalar differential group delay from the magnitude of the polarization mode dispersion vector, the frequency derivative of the scalar differential group delay  $\frac{d|\vec{\tau}|}{d\omega}$  being a scalar second-order polarization mode dispersion function;

calculating a first result, according to  $\left\langle \left| \frac{d|\vec{\tau}|}{d\omega} \right|^{\frac{1}{2}} \right\rangle$ , where  $|\tau|$  is in units of second and  $\omega$  is

a frequency in units of radian/second; and

multiplying a proportionality coefficient  $B_2$  by the first result to calculate the mean differential group delay, in accordance with the following equation:

$$B_{2}\left\langle \left| \frac{d|\vec{\tau}|}{d\omega} \right|^{\frac{1}{2}} \right\rangle = \langle \tau \rangle, \tag{26}$$

where  $B_2$  is dimensionless,  $\tau$  and  $\langle \tau \rangle$  are in units of second,  $\omega$  is in units of radian/second,

and 
$$\frac{d|\vec{\tau}|}{d\omega}$$
 is in units of second<sup>2</sup>.

- 17. The method of Claim 16, wherein  $B_2$  is substantially equal to 2.64.
- 18. The method of Claim 16, wherein the frequency-domain polarization mode dispersion measurement apparatus comprises one of a polarimetric device and a Fixed Analyzer device.
- 19. The method of Claim 16, wherein the at least one length of optical fiber is a single optical fiber link.
- 20. The method of Claim 16, wherein the at least one length of optical fiber is an optical fiber route.
- 21. A method for measuring a mean square differential group delay  $\tau^2_{RMS}$  of at least one length of optical fiber, comprising the steps of:

measuring a polarization mode dispersion vector as a function of frequency, using a frequency-domain polarization mode dispersion measurement apparatus;

calculating a second-order polarization mode dispersion vector  $\vec{\tau}_{\omega}$  as a function of frequency by calculating a derivative of the polarization mode dispersion vector with respect to frequency  $\omega$ ;

calculating the mean of the magnitude of the second-order polarization mode dispersion vector  $|\vec{\tau}_{\omega}|$  to obtain a first result, according to  $\langle |\vec{\tau}_{\omega}| \rangle$ ; and

multiplying a proportionality coefficient  $A_I$  by the first result to calculate the mean square differential group delay, in accordance with the following equation:

$$A_1 \left\langle \left| \vec{\tau}_{\omega} \right| \right\rangle = \tau_{RMS}^2, \tag{20}$$

where  $A_I$  is dimensionless,  $|\vec{\tau}_{\omega}|$  is in units of second<sup>2</sup> and  $\tau^2_{RMS}$  is in units of second<sup>2</sup>.

- 22. The method of Claim 21, wherein  $A_I$  is substantially equal to 2.02.
- 23. The method of Claim 21, wherein the frequency-domain polarization mode dispersion measurement apparatus comprises one of a polarimetric device and a Fixed Analyzer device.
- 24. The method of Claim 21, wherein the at least one length of optical fiber is a single optical fiber link.
- 25. The method of Claim 21, wherein the at least one length of optical fiber is an optical fiber route.
- 26. A method for measuring a mean square differential group delay  $\tau^2_{RMS}$  of at least one length of optical fiber, comprising the steps of:

measuring a magnitude of a polarization mode dispersion vector as a function of frequency using a frequency-domain polarization mode dispersion measurement apparatus, the magnitude of the polarization mode dispersion vector being a scalar differential group delay;

calculating a frequency derivative of the scalar differential group delay from the magnitude of the polarization mode dispersion vector, the frequency derivative of the scalar

differential group delay  $\frac{d|\vec{\tau}|}{d\omega}$  being a scalar second-order polarization mode dispersion function;

calculating a first result, according to 
$$\left\langle \left| \frac{d|\bar{\tau}|}{d\omega} \right| \right\rangle$$
; and

multiplying a proportionality coefficient  $B_I$  by the first result to calculate the mean square differential group delay, in accordance with the following equation:

$$B_{1}\left\langle \left| \frac{d|\vec{\tau}|}{d\omega} \right| \right\rangle = \tau_{\text{\tiny RMS}}^{2}, \tag{25}$$

where  $B_1$  is dimensionless, and  $\frac{d|\vec{\tau}|}{d\omega}$  is in units of second<sup>2</sup>.

- 27. The method of Claim 26, wherein  $B_I$  is substantially equal to 6.80.
- 28. The method of Claim 26, wherein the frequency-domain polarization mode dispersion measurement apparatus comprises one of a polarimetric device and a Fixed Analyzer device.
- 29. The method of Claim 26, wherein the at least one length of optical fiber is a single optical fiber link.
- 30. The method of Claim 26, wherein the at least one length of optical fiber is an optical fiber route.
- 31. A method for measuring a mean polarization mode dispersion of at least one length of optical fiber, using a source of bandwidth B, comprising the steps of:

collecting polarization mode dispersion data as a function of frequency from a frequency-domain polarization mode dispersion measurement apparatus;

extracting one of a vector and a scalar frequency-dependent function from the polarization mode dispersion data, by applying a frequency-domain polarization mode dispersion technique, the one of the vector and the scalar function being one of a first-order and a second-order polarization mode dispersion function;

applying a systematic correction to the one of the vector and the scalar frequency-dependent function, the systematic correction minimizing a systematic error caused by bandwidth B; and wherein

applying the systematic correction results in a derivation of one of a mean differential group delay  $\langle \tau \rangle$  and a mean square differential group delay  $\tau^2_{RMS}$ .

32. A method of measuring a mean differential group delay  $\langle \tau \rangle$  of a length of optical fiber comprising the steps of:

deriving a first mean  $\langle \tau \rangle$  in accordance with equation (21) and Claim 11;

deriving a second mean  $\langle \tau \rangle$  in accordance with equation (26) and Claim 16; deriving a linear equation of the first mean  $\langle \tau \rangle$  and the second mean  $\langle \tau \rangle$  to calculate a combined mean  $\langle \tau \rangle$ , wherein a sum of coefficients of the linear equation is substantially equal to one.

33. A method of measuring a mean square differential group delay  $\tau^2_{RMS}$  of a length of optical fiber comprising the steps of:

deriving a first mean square differential group delay  $\tau^2_{RMS}$  in accordance with equation (20) and Claim 21;

deriving a second mean square differential group delay  $\tau^2_{RMS}$  in accordance with equation (25) and Claim 26;

deriving a linear equation of the first mean square differential group delay  $\tau^2_{RMS}$  and the second mean square differential group delay  $\tau^2_{RMS}$  to calculate a combined mean square differential group delay  $\tau^2_{RMS}$ , wherein a sum of coefficients of the linear equation is substantially equal to one.